

Instrumentation, Analytical Techniques and Sampling

ENHL 232

Lecture 1



Introduction

Objectives of the session:

- Provide an overview about
 - The basic units of metric system
 - Concentration units
 - Dilution calculations
 - Interpretation of data
 - Statistical Calculations

The Importance of Units

- Numbers are meaningless without units
- The basic units of metric system:
 - Length in meter
 - Mass in kilogram
 - Volume in liter



Unit of Prefixes and their Values

| Prefix | Symbol | Exponential value |
|--------|--------|-------------------|
| Kilo | k | 10^3 |
| Hecto | h | 10^2 |
| Deca | da | 10 |
| Deci | d | 10^{-1} |
| Centi | c | 10^{-2} |
| Milli | m | 10^{-3} |
| Micro | μ | 10^{-6} |
| Nano | n | 10^{-9} |
| Pico | p | 10^{-12} |

Concentration Units

- Molarity (M)
 - The number of moles of a certain species contained in one liter of the solution
 -
 -

Concentration Units

- Normality (N)
 - Normality is the number of equivalents of solute per liter of a solution
 - $N = \text{equivalent of solute} / v \text{ of solution (l)}$
 - Normality of a solution depends on the reaction taking place
 - For normality to be calculated the stoichiometric equation must be known

Concentration Units

- - where X may be
 - acidity of a base
 - basicity of an acid
 - number of electrons gained or lost by a redox reagent

Types of reactions

- Acid-base neutralization
 -
- Oxidation-reduction reactions
 -
- Precipitate formation
- Complex formation

pFunction or the negative logarithm function

- - Mostly, the function is the concentration of the studied species
 - The symbol of the studied species in terms of its concentration is enclosed in brackets
 -
 -
 -

Percent

- Weight percent
 - weight percent = $(\text{weight solute}/\text{weight solution}) \times 100$ with same weight units such as gram-gram, mg-mg, Kg-Kg
 - For solid such as ores or tissue samples:
 - Weight percent = $(\text{grams substance determined}/\text{grams total sample}) \times 100$

Percent

- Volume percent
 - Used if both the solute and the solvent are liquids
 - Volume percent = $(\text{volume solute}/\text{volume solution}) \times 100$ with same volume units such as ml-ml or liter-liter
- Weight-volume percent
 - Used in the preparation of approximate concentrations of solutions:
 - Weight-volume percent = $(\text{g solute}/\text{ml solution}) \times 100$

Parts per thousand, parts per million, and parts per billion

- 1 ppm = 1 g of analyte per million grams of water
- 1 ppb = 1 g of analyte per billion grams of water

Parts per unit methods of expressing concentrations and equivalent expressions ¹³

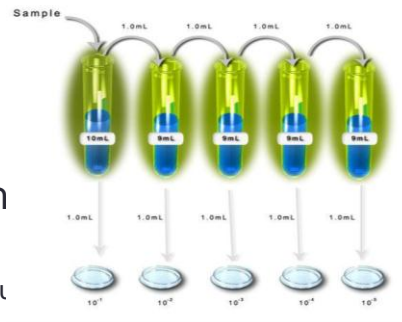
| Expression | Parts per unit part | Equivalent quantities | |
|--------------------------|---------------------|-----------------------|----------------------|
| | | Solids | Liquids |
| Percent (%) | 10^2 | g/100 g | g/100 ml |
| Parts per thousand (ppt) | 10^3 | g/1000 g | g/1000 ml |
| | | g/Kg | g/L |
| | | mg/g | mg/ml |
| Milligram percent (mg %) | 10^5 | g/10 ⁵ g | g/10 ⁵ ml |
| | | g/100 Kg | g/100 L |
| | | mg/100 g | mg/100 ml |
| Parts per million (ppm) | 10^6 | g/10 ⁶ g | g/10 ⁶ ml |
| | | g/10 ³ Kg | g/10 ³ L |
| | | mg/Kg | mg/L |
| | | µg/g | µg/ml |
| Parts per billion (ppb) | 10^9 | g/10 ⁹ g | g/10 ⁹ ml |
| | | g/10 ⁶ Kg | g/10 ⁶ L |
| | | mg/10 ³ Kg | mg/10 ³ L |
| | | µg/Kg | µg/L |
| | | ng/g | ng/ml |

Dilution Calculations ¹⁴

- It is often necessary for experimental needs to dilute our sample so as to have a lower concentration

The dilution process involves adding water to a known concentration and volume of the sample that is a higher concentration value

- Number of moles in diluted sample = n_i sample



Interpretation of Data

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- Precision and accuracy

Precision: the variability among replicate measurements, i.e., how close the values in a series of results are to each other

Accuracy: the difference between the obtained value and the true value

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SUPPOSE YOU MEASURED THE MASS OF A ROCK TO BE 8.2 GRAMS AND THE VOLUME TO BE 2.3 CM³.

HOW ACCURATELY CAN YOU DETERMINE ITS DENSITY?

$$\text{Density} = \text{Mass/Volume} = 8.2 \text{ gm}/2.3 \text{ cm}^3 = 3.56521739 \text{ gm/ cm}^3$$

Mass measured to 2 significant digits

What's wrong with this calculation?

Volume measured to 2 significant digits

Not science but fiction!

Maybe this doesn't look as impressive, but it is a better answer.

$$\text{Density} = \text{Mass/Volume} = 8.2 \text{ gm}/2.3 \text{ cm}^3 = 3.57 \text{ gm/ cm}^3$$

$$\text{Density} = 3.6 \text{ gm/ cm}^3$$

It is better to keep only the number of digits of your weakest measurement for your final answer.

No fictional digits – well, maybe the 7 is stretching it. It is reasonable to carry an extra digit or two in intermediate calculations

Interpretation of Data

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- There are three rules on determining how many significant figures are in a number:

– **Non-zero digits are always significant.**

Significant Digits

Rules:
1. All non-zero digits are significant

– **Any zeros between two significant digits are significant.**

| Number | Significant Digits |
|---------|--------------------|
| 28.09 | 4 |
| 1008.91 | 6 |
| 3.005 | 4 |
| 2.03 | 3 |

– **A final zero in the decimal part is significant.**

Rules for Counting Significant Digits:

- All non-zero digits and any zeros contained between non-zero digits count.
300042 = 6 significant digits
- Leading zeros don't count.
0.00034 = 2 significant digits
- Trailing zeros count if there is a decimal point.
0.0002500 = 4 significant digits
- Trailing zeros may or may not count if there is no decimal point, so we go with the most conservative answer.
190000 = 2 significant digits (could be up to 6)

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Interpretation of Data

- 26.38 would have four significant figures and 7.94 would have three
- 0.005 (5.00×10^{-3})
- 0.0304 (3.040×10^{-2})

Interpretation of Data

- Absolute and relative uncertainty
 - The uncertainty of a value may be expressed in absolute or relative terms

Interpretation of Data

- Significant figures in numerical computations
 - A chain is only as strong as its weakest link
 - For addition and subtraction, the weak link is the number of decimal places in the number with the smallest number of decimal places
 -

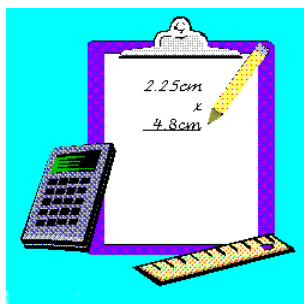
Interpretation of Data

- The weak link for multiplication and division is the number of significant figures in the number with the smallest number of significant figures

Interpretation of Data

- Example:
 $8.9 \text{ g} / 12.01 \text{ g/mol} = 0.74 \text{ mol}$

$$\begin{array}{r} 8.9444 \text{ g} \\ +18.52 \text{ g} \\ \hline 27.46 \text{ g} \end{array}$$



Interpretation of Data

- Rounding data
 - Always round the computed results of a chemical analysis in an appropriate way
 - A good guide to follow when rounding a 5 is always to round to the nearest even number 6

Calibration

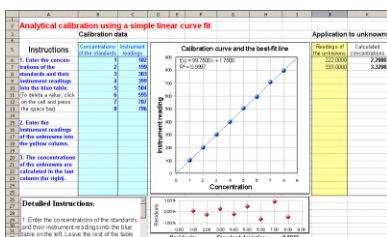
- Making measurements with any analytical method instrument requires calibration to ensure the accuracy of the measurement



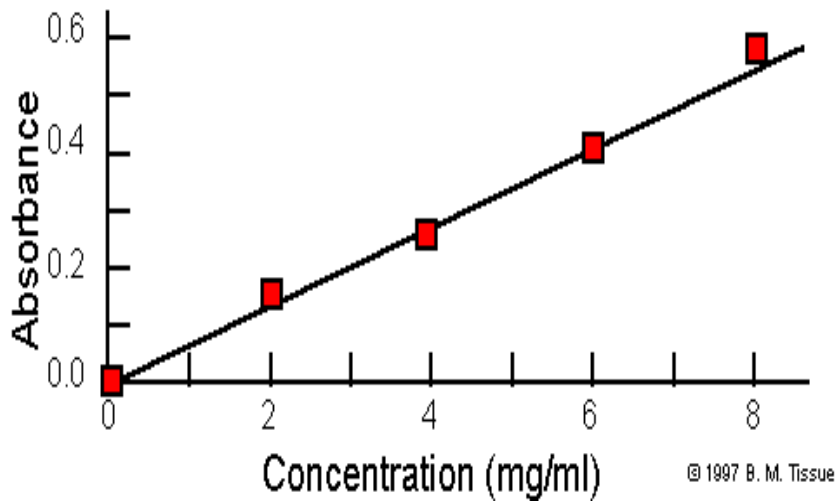
- Two common calibration procedures:

Working curve:

Standard addition



Working Curve



Standard Addition

- An analyst usually divides the unknown sample into two portions, so that a known amount of the analyte (a spike) can be added to one portion
- The original and the original plus spike, are then analyzed
- The sample with the spike will show a larger analytical response than the original sample due to the additional amount of analyte added to it

Internal Standard Method

- Instead of using the analyte itself as the calibrant, another substance is used
- It is possible to determine the analyte concentration from a single measurement
- Any losses of analyte will be reflected in similar losses of internal standard

Introduction to Statistics

- The average is synonymous with the arithmetic mean
 - Obtained by adding the results of a number of replications and dividing this sum by the number of replications

$$\bar{X} = \frac{\sum_{i=1}^N X_i}{N}$$

Introduction to Statistics

- The average is an important component of reported results but on itself is insufficient
- HOWEVER the extent of the variations within any set of values should also be considered
- From the deviations an average deviation, may be calculated
- The average deviation is the arithmetic mean of the absolute values of the individual deviations

Introduction to Statistics

- Another mean of expressing precision is with standard deviations
 - This is defined as the square root of the sum of the squares of the absolute deviations of the individual samples divided by one less than the number of samples

$$S = \sqrt{\frac{\sum_{i=1}^N (x_i - \bar{X})^2}{N - 1}}$$

Standard Deviation and Variance

Deviation just means how far from the normal

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- Standard Deviation
- The Standard Deviation is a measure of how spread out numbers are.
- Its symbol is σ (the greek letter sigma)
- The formula is easy: it is the square root of the Variance. So now you ask, "What is the Variance?"
- Variance
- The Variance is defined as:
 - The average of the squared differences from the Mean.
 - To calculate the variance follow these steps:
 - Work out the [Mean](#) (the simple average of the numbers) Then for each number: subtract the Mean and square the result (the *squared difference*). Then work out the average of those squared differences. ([Why Square?](#))
- Example
 - You and your friends have just measured the heights of your dogs (in millimeters):
 - The heights (at the shoulders) are: 600mm, 470mm, 170mm, 430mm and 300mm.
 - Find out the Mean, the Variance, and the Standard Deviation.
 - Your first step is to find the Mean:
 - Answer:
 - Mean = $600 + 470 + 170 + 430 + 300 = 1970 = 3945$
 - so the mean (average) height is 394 mm. Let's plot this on the chart: Now, we calculate each dogs difference from the Mean:
 - To calculate the Variance, take each difference, square it, and then average the result:
 - So, the Variance is 21,704.
 - And the Standard Deviation is just the square root of Variance, so:
 - Standard Deviation: $\sigma = \sqrt{21,704} = 147.32... = 147$ (to the nearest mm)
 - And the good thing about the Standard Deviation is that it is useful. Now we can show which heights are within one Standard Deviation (147mm) of the Mean:
 - So, using the Standard Deviation we have a "standard" way of knowing what is normal, and what is extra large or extra small.
 - Rottweilers are tall dogs. And Dachshunds are a bit short ... but don't tell them!
 - Now try the [Standard Deviation Calculator](#).

But ... there is a small change with Sample Data

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- Our example was for a Population (the 5 dogs were the only dogs we were interested in).
- But if the data is a Sample (a selection taken from a bigger Population), then the calculation changes!
- When you have "N" data values that are:
 - The Population: divide by N when calculating Variance (like we did)
 - A Sample: divide by N-1 when calculating Variance
 - All other calculations stay the same, including how we calculated the mean.
 - Example: if our 5 dogs were just a sample of a bigger population of dogs, we would divide by 4 instead of 5 like this:
 - Sample Variance = $108,520 / 4 = 27,130$
 - Sample Standard Deviation = $\sqrt{27,130} = 164$ (to the nearest mm)
 - Think of it as a "correction" when your data is only a sample.
 - Formulas
 - Here are the two formulas, explained at [Standard Deviation Formulas](#) if you want to know more:
- The "Population Standard Deviation":
 - The "Sample Standard Deviation": Looks complicated, but the important change is to divide by N-1 (instead of N) when calculating a Sample Variance.
- *Footnote: Why *square* the differences?
 - If we just added up the differences from the mean ... the negatives would cancel the positives:
 - $4 + 4 - 4 - 4 = 0$ So that won't work. How about we use [absolute values](#)?
 - $|4| + |4| + |-4| + |-4| = 4 + 4 + 4 + 4 = 16$ That looks good, but what about this case:
 - $|7| + |1| + |-6| + |-2| = 7 + 1 + 6 + 2 = 16$ Oh No! It also gives a value of 16, Even though the differences are more spread out!
 - So let us try squaring each difference (and taking the square root at the end):
 - $\sqrt{4^2 + 4^2 + 4^2 + 4^2} = \sqrt{64} = 4$ That looks good, but what about this case:
 - $\sqrt{7^2 + 1^2 + 6^2 + 2^2} = \sqrt{90} = 9.49$ That is nice! The Standard Deviation is bigger when the differences are more spread out ... just what we want!
 - In fact this method is a similar idea to [distance between points](#), just applied in a different way.
 - And it is easier to use algebra on squares and square roots than absolute values, which makes the standard deviation easy to use in other areas of mathematics.

Questions

